## Volume of Solids



Name:
To be able to calculate the volume of spheres, pyramids and cones Calculators allowed

## SPHERE

## Example

A sphere has radius 5 cm . Find the volume.

$$
\mathrm{V}=\frac{4}{3} \pi \mathrm{r}^{3} \quad \begin{aligned}
& \mathrm{r}=5 \\
& \mathrm{~V}=4 \times \Pi \times 5^{3} \div 3 \\
& \\
& \mathrm{~V}=4 \times \Pi \times 125 \div 3 \\
& \\
& \mathrm{~V}=500 \Pi \div 3=\underline{523.60}(2 \mathrm{dp})
\end{aligned}
$$

## QUESTIONS

| 1. $\mathrm{r}=4$ | 2. $\mathrm{r}=10$ |
| :---: | :---: |
| $\mathrm{V}=4 \times \Pi \times 4^{3} \div 3$ | $\mathrm{V}=4 \times \Pi \times 10^{3} \div 3$ |
| $\mathrm{V}=4 \times \Pi \times 64 \div 3$ | $\mathrm{V}=4 \times \Pi \times 1000 \div 3$ |
| $\mathrm{V}=256 \Pi \div 3$ | $\mathrm{V}=$ ___ $\Pi \div 3$ |
| $\mathrm{V}=$ _ | $\mathrm{V}=\ldots$ _ (2dp) |
| 3. $\mathrm{r}=7$ | 4. $\mathrm{r}=6$ |
| $\mathrm{V}=4 \times \Pi \times 7^{3} \div 3$ | $\mathrm{V}=4 \times \Pi \times$ __ $^{3} \div 3$ |
| $\mathrm{V}=4 \times \Pi \times$ ___ $\div 3$ | $\mathrm{V}=4 \times \Pi \times \ldots \div 3$ |
| $\mathrm{V}=$ ___ $\Pi \div 3$ | $\mathrm{V}=$ ___ $\Pi \div 3$ |
| $\mathrm{V}=\ldots \quad \text { (2dp) }$ | $\mathrm{V}=\ldots \quad(2 \mathrm{dp})$ |
| 5. $\mathrm{r}=11$ | 6. $\mathrm{r}=8$ |
| $\mathrm{V}=4 \times \Pi \times \_^{3} \div$ | $\mathrm{V}=\__{\quad} \times \Pi \times \ldots^{3} \div$ |
| $\mathrm{V}=4 \times \Pi \times \ldots$ | $\mathrm{V}=$ ___ $\times \Pi \times \ldots \ldots$ |
| $V=\_\quad \Pi \div$ | $\mathrm{V}=\ldots \quad \Pi \div$ |
| $\mathrm{V}=\ldots \ldots$ _ (2dp) | $\mathrm{V}=\ldots \quad \text { (2dp) }$ |

## Extension

Find the volume of a sphere with radius 13 cm

## CONE

Example


A cone has radius 5 cm and height 4 cm . Find the volume.
$\mathrm{r}=5, \mathrm{~h}=4$

$$
\begin{aligned}
& V=\Pi \times 5^{2} \times 4 \div 3 \\
& V=\Pi \times 25 \times 4 \div 3 \\
& V=100 \Pi \div 3=\underline{104.72}(2 \mathrm{dp})
\end{aligned}
$$

## QUESTIONS

| 1. $\mathrm{r}=4, \mathrm{~h}=7$ | 2. $\mathrm{r}=10, \mathrm{~h}=7$ |
| :---: | :---: |
| $\mathrm{V}=\Pi \times 4^{2} \times 7 \div 3$ | $\mathrm{V}=\Pi \times 10^{2} \times 7 \div 3$ |
| $\mathrm{V}=\Pi \times 16 \times 7 \div 3$ | $\mathrm{V}=\Pi \times 100 \times 7 \div 3$ |
| $\mathrm{V}=112 \Pi \div 3$ | $V=\ldots \quad \Pi \div 3$ |
| $\mathrm{V}=$ [__ (2dp) | $\mathrm{V}=\ldots \ldots$ ( 2 dp ) |
| 3. $\mathrm{r}=9, \mathrm{~h}=2$ | 4. $\mathrm{r}=6, \mathrm{~h}=12$ |
| $\mathrm{V}=\Pi \times 9^{2} \times 2 \div 3$ | $\mathrm{V}=\Pi \times \_^{2} \times 12 \div 3$ |
| $\mathrm{V}=\Pi \times \ldots \times 2 \div 3$ | $\mathrm{V}=\Pi \times \ldots \times 12 \div 3$ |
| $\mathrm{V}=$ ___ $\Pi \div 3$ | $\mathrm{V}=\ldots \quad \Pi \div 3$ |
| $\mathrm{V}=\ldots \quad \text { (2dp) }$ | $\mathrm{V}=\ldots \quad \text { (2dp) }$ |
| 5. $\mathrm{r}=11, \mathrm{~h}=5$ | 6. $\mathrm{r}=11, \mathrm{~h}=8$ |
| $\mathrm{V}=\Pi \times \_^{2} \times 5 \div 3$ | $\mathrm{V}=\Pi \times \__{1}{ }^{2} \times \__{ـ} \div 3$ |
| $\mathrm{V}=\Pi \times \ldots \ldots \ldots \ldots 3$ | $V=\Pi \times \ldots \times \ldots \div 3$ |
| $\mathrm{V}=$ ___ $\Pi \div 3$ | $V=\ldots \quad \Pi \div 3$ |
| $\mathrm{V}=\ldots \quad \text { (2dp) }$ | $\mathrm{V}=\ldots \quad(2 \mathrm{dp})$ |

## Hints

The $\Pi \times r^{2}$ bit comes
from the area of the base

Sketch the cone if you have trouble remembering which measurement goes where.

## Extension

Find the volume of a cone with radius 13 cm and height 10 cm

## PYRAMID

## Example

A pyramid has a 5 cm square base and height 7 cm . Find the volume.
volume $=\frac{1}{3}$ base area $x$ height Base $=5 \times 5=25$


$$
\begin{aligned}
& \mathrm{H}=7 \\
& \mathrm{~V}=25 \times 7 \div 3 \\
& \mathrm{~V}=175 \div 3 \\
& \mathrm{~V}=\underline{58.33}(2 \mathrm{dp})
\end{aligned}
$$

## Hints

The base can be any 2D shape, you will need to adjust your calculation to fit.

Sketch the pyramid if you have trouble visualizing the base shape.

## QUESTIONS

| $1 \mathrm{lh}=5$ | 2. $\mathrm{h}=8$ |
| :---: | :---: |
| Base $=\mathbf{4}$ by 6 rectangle | Base $=\mathbf{7}$ by 4 rectangle |
| Base $=4 \times 6=24$ | Base $=7 \times 4=$ |
| $\mathrm{V}=24 \times 5 \div 3$ | $\mathrm{V}=$ ___ $\times 8 \div 3$ |
| $\mathrm{V}=120 \div 3$ | $\mathrm{V}=\ldots \ldots \ldots 3$ |
| $\mathrm{V}=\ldots$ | $\mathrm{V}=\ldots \ldots$ (2dp) |
| 3. $\mathrm{h}=10$ | 4. $\mathrm{h}=5$ |
| Base $=9$ by 4 triangle | Base = $\mathbf{1 2}$ by $\mathbf{6}$ triangle |
| Base $=9 \times 4 \div 2=$ | Base $=12 \times \ldots \div 2=$ |
| $\mathrm{V}=$ ___ $\times \ldots \div 3$ | $\mathrm{V}=\ldots \ldots \times \ldots 3$ |
| $\mathrm{V}=\ldots \ldots \div 3$ | $\mathrm{V}=\ldots \ldots+3$ |
| $\mathrm{V}=\ldots$ | $\mathrm{V}=\ldots \quad(2 \mathrm{dp})$ |

## Extension

Find the volume of a pyramid with height 10 cm and $a$ triangular base. The triangle is right angled with sides 3, 4, 5 cm

