

Small steps in Direct Proportion

Each question takes you through how to form a direct proportion equation, gradually decreasing the support.

Example

W is directly proportional to V. When $W = 42$, $V = 7$. Find W when $V = 10$.

Basic statement: $W \propto V$

Proportion equation: $W = kV$

Substitute to find k: $42 = k \times 7$

$$k = 42 \div 7 = 6$$

State equation: $W = 6V$

Use equation to solve the problem: $V = 10$ $W = 6 \times 10 = \mathbf{60}$

Questions: Fill in the gaps

1. T is directly proportional to C. When $T = 14$, $C = 3.5$. Find T when $C = 8$.

Basic statement: $T \propto C$

Proportion equation: $T = kC$

Substitute to find k: $14 = k \times 3.5$

$$k = 14 \div 3.5 = 4$$

State equation: $T = 4C$

Use equation to solve the problem: $C = 8$ $T = 4 \times \underline{\quad} = \underline{\quad}$

2. x varies directly with t. When $x = 15$, $t = 6$. Find x when $t = 6$.

Basic statement: $x \propto t$

Proportion equation: $x = kt$

Substitute to find k: $15 = k \times 6$

$$k = 15 \div 6 = 2.5$$

State equation: $x = 2.5t$

Use equation to solve the problem: $t = 6$ $x = \underline{\quad} \times \underline{\quad} = \underline{\quad}$

3. A is in direct to proportion to B. When $A = -12$, $B = 4$. Find A when $B = 9$.

Basic statement: $A \propto B$

Proportion equation: $A = kB$

Substitute to find k: $-12 = k \times 4$

$$k = -12 \div 4 = \underline{\quad}$$

State equation: $A = \underline{\quad}B$

Use equation to solve the problem: $B = 9$ $A = \underline{\quad} \times \underline{\quad} = \underline{\quad}$

4. J varies in proportion to M. When $J = 2$, $M = 20$. Find J when $M = 13$.

Basic statement: $J \propto M$

Proportion equation: $J = k M$

Substitute to find k: $2 = k \times 20$

$$k = \underline{\quad} \div \underline{\quad} = \underline{\quad}$$

State equation: $J = \underline{\hspace{2cm}}$

Use equation to solve the problem: $M = 13$ $J = \underline{\hspace{2cm}}$

5. P is directly proportional to Q. When $P = 360$, $Q = 90$. Find P when $Q = 15$.

Basic statement: $P \propto Q$

Proportion equation: $P = k Q$

Substitute to find k: $\underline{\quad} = k \times \underline{\quad}$

$$k = \underline{\quad} \div \underline{\quad} = \underline{\quad}$$

State equation: $P = \underline{\hspace{2cm}}$

Use equation to solve the problem: $Q = \underline{\quad}$ $P = \underline{\hspace{2cm}}$

6. m is in proportional to r. When $m = \frac{1}{2}$, $r = \frac{1}{4}$. Find m when $r = \frac{3}{4}$.

Basic statement: $m \propto r$

Proportion equation: $m = \underline{\hspace{2cm}}$

Substitute to find k: $\underline{\quad} = k \times \underline{\quad}$

$$k = \underline{\quad} \div \underline{\quad} = \underline{\quad}$$

State equation: $\underline{\hspace{2cm}}$

Use equation to solve the problem: $\underline{\quad} = \underline{\quad}$ $\underline{\quad} = \underline{\hspace{2cm}}$

7. y is directly proportional to x. When $y = 72$, $x = 48$. Find y when $x = 15$.

Basic statement: $\underline{\quad} \propto \underline{\quad}$

Proportion equation: $y = \underline{\hspace{2cm}}$

Substitute to find k: $\underline{\quad} = k \times \underline{\quad}$

$$k = \underline{\quad} \div \underline{\quad} = \underline{\quad}$$

State equation: $\underline{\hspace{2cm}}$

Use equation to solve the problem: $\underline{\hspace{2cm}}$

8. E varies directly with to G. When $E = -18$, $G = -3$. Find E when $G = 7$.

Basic statement:

Proportion equation:

Substitute to find k:

State equation:

Use equation to solve the problem:

Now consider how to use this structure to solve other direct proportion questions.

Extension: How can you adapt this technique for problems such as “y is proportional to the square of x. When y is 75, x is 5. Find the value of y when x is 7”

Small steps in Direct Proportion: Solutions

1. 32
2. 15
3. -27
4. 1.3
5. 60
6. 1.5
7. 22.5
8. 42